How to Derive an Electronic Functional Programming Exam from a Paper Exam with Proofs and Programming Tasks

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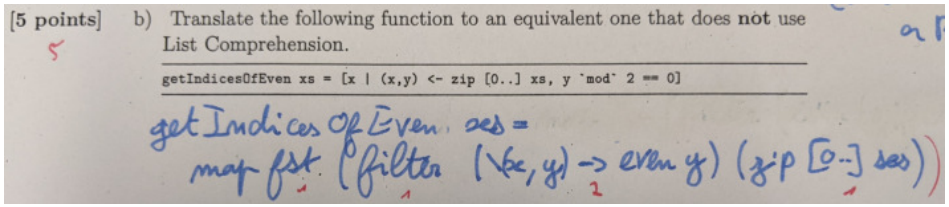
Motivation


[5 points] b) Translate the following function to an equivalent one that does not use List Comprehension.

```
getIndicesOfEven xs = [x | (x,y) <- zip [0..] xs, y `mod` 2 == 0]
```

```
getIndicesOfEven xes =
  map fst (filter (\(x,y) -> even y) (zip [0..] xes))
```

Figure 1: Paper Exam

- Complex, constructively aligned tasks
- High grading effort
- Handwritten code . . .

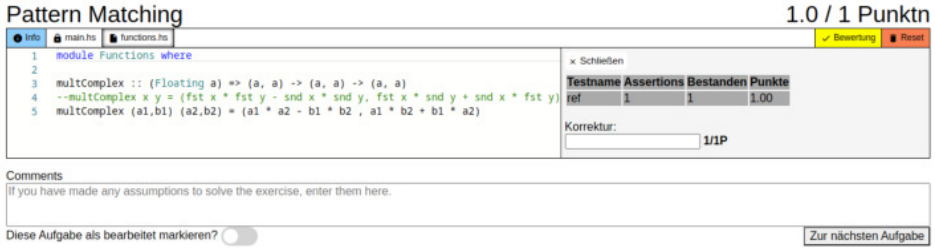


Figure 2: E-Exam

- Complex, more constructively aligned tasks
- Automated grading
- Familiar working environment

Outline

1. Analysis of our Pre-E-Exam FP Course
2. Realization
   - Programming Tasks
   - New Algorithm to Evaluate Proof Puzzles
3. Summary & Future Work

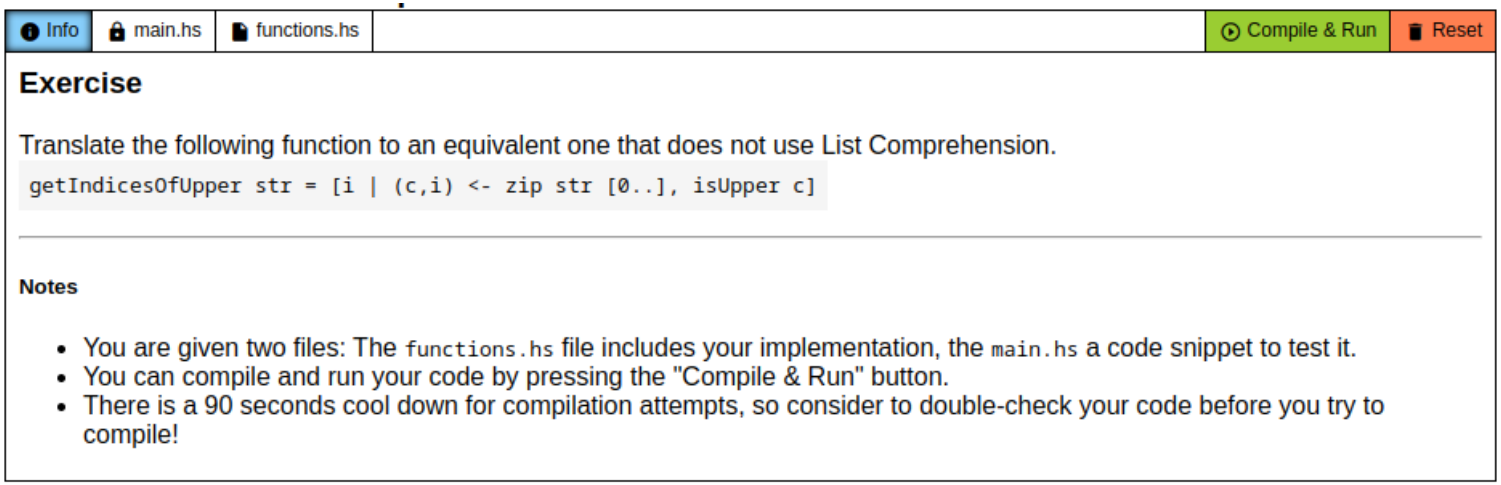
Analysis of our Pre-E-Exam FP Course

Table 1: Excerpt from analysis results

Task	Learning Objective	Type
1a	K_1, K_2, K_4	snippet
1b	K_1, K_2, K_4	multiple choice
2a	K_1, K_2, K_3	single choice, snippet
2b	K_1, K_2, S_2, S_3	code
3a	K_1, K_2, K_3, K_4	single choice, snippet
3b	K_1, K_2, K_4, S_3	code
4a	K_1, K_2	text
...	...	...

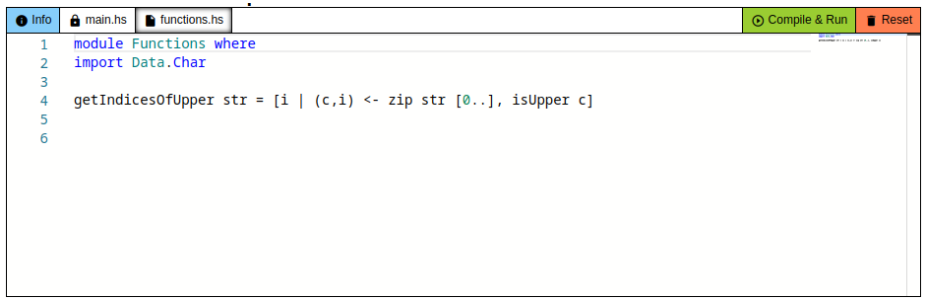
Realization

Programming Tasks



Task description

main.hs

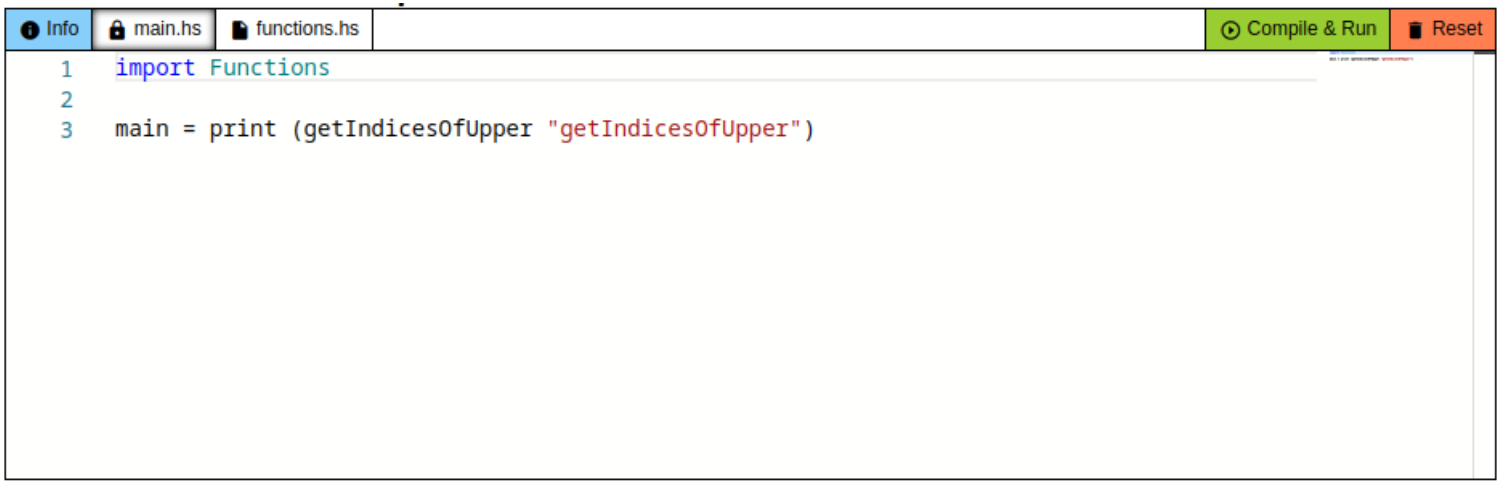


functions.hs

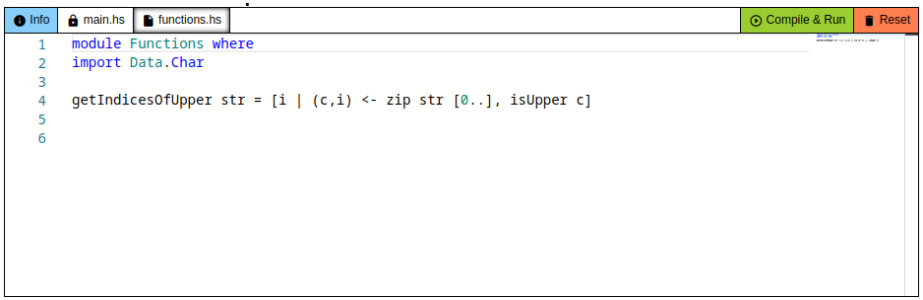
Figure 3: Programming task

Realization

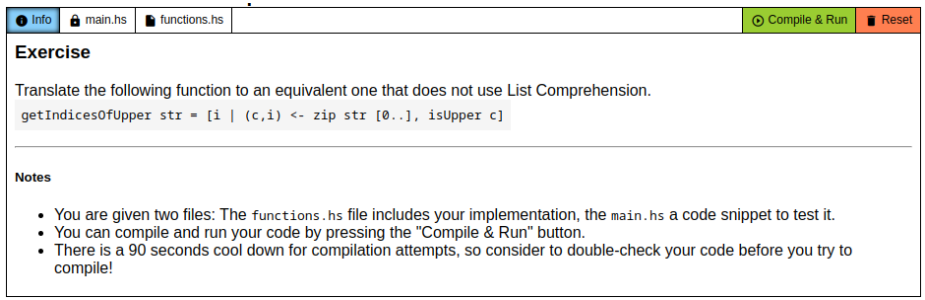
Programming Tasks



main.hs



functions.hs

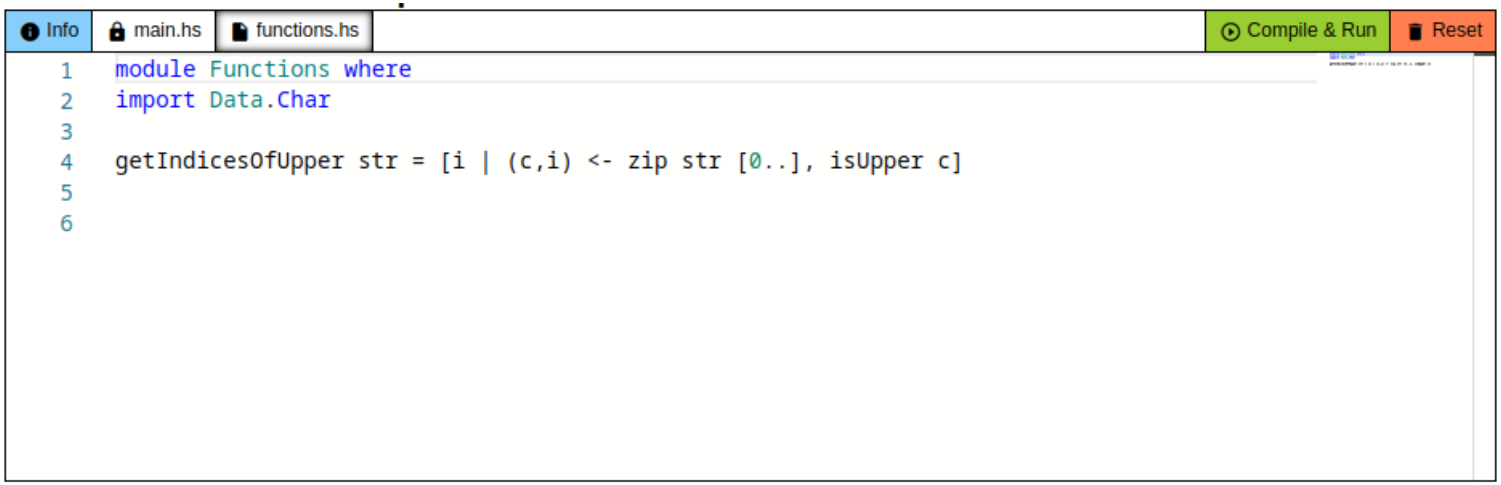


Task description

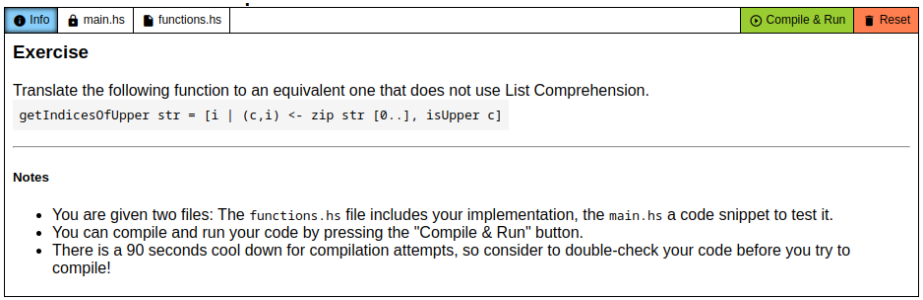
Figure 3: Programming task

Realization

Programming Tasks



functions.hs



Task description

main.hs

Figure 3: Programming task

Realization

Programming Tasks – Static Analysis of Student Code

Listing 1: Example of quicksort in Haskell[1]

```haskell
quicksort :: Ord a => [a] -> [a]
quicksort [] = []
quicksort (p:xs) = (quicksort ls) ++ [p] ++ (quicksort gs)
  where ls = filter (< p) xs
        gs = filter (>= p) xs
```

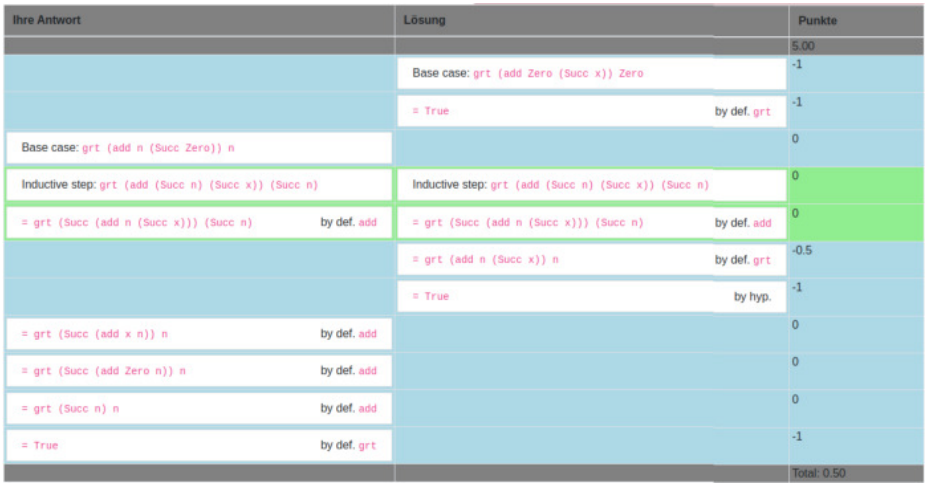
Listing 2: Corresponding output of analyzer

```
{ "functions": [{
  "name": "quicksort",
  "patMatch": true,
  "guards": false,
  "listComprehension": false,
  "hasIf": false,
  "hasCase": false,
  "args": [ "p", "xs" ],
  "calledFns": [ "quicksort", "++", "filter", "<", ">=" ],
  "declaredFns": [ ]
}]}
```

[1] https://wiki.haskell.org/Introduction#Quicksort_in_Haskell

Realization

New Algorithm to Evaluate Proof Puzzles



Ihre Antwort	Lösung	Punkte
		5.00
	Base case: `grt (add Zero (Succ x)) Zero`	-1
	`= True` by def. `grt`	-1
Base case: `grt (add n (Succ Zero)) n`		0
Inductive step: `grt (add (Succ n) (Succ x)) (Succ n)`	Inductive step: `grt (add (Succ n) (Succ x)) (Succ n)`	0
`= grt (Succ (add n (Succ x))) (Succ n)` by def. `add`	`= grt (Succ (add n (Succ x))) (Succ n)` by def. `add`	0
	`= grt (add n (Succ x)) n` by def. `grt`	-0.5
	`= True` by hyp.	-1
`= grt (Succ (add x n)) n` by def. `add`		0
`= grt (Succ (add Zero n)) n` by def. `add`		0
`= grt (Succ n) n` by def. `add`		0
`= True` by def. `grt`		-1
		Total: 0.50

(a) Student A

Ihre Antwort	Lösung	Punkte
		5.00
Base case: `grt (add Zero (Succ x)) Zero`	Base case: `grt (add Zero (Succ x)) Zero`	0
`= grt (Succ x) Zero` by def. `grt`		0
Inductive step: `grt (add (Succ Zero) (Succ x)) (Succ Zero)`		0
`= grt (Succ (Succ x)) (Succ Zero)` by def. `add`		0
`= True` by def. `grt`	`= True` by def. `grt`	0
	Inductive step: `grt (add (Succ n) (Succ x)) (Succ n)`	-1
	`= grt (Succ (add n (Succ x))) (Succ n)` by def. `add`	-0.5
	`= grt (add n (Succ x)) n` by def. `grt`	-0.5
	`= True` by hyp.	-1
		Total: 2.00

(b) Student B

Figure 4: Example of unfair grading with old algorithm

- Evaluation algorithm based on **edit-distance** between given and correct solution

Realization

New Algorithm to Evaluate Proof Puzzles

Ihre Antwort	Lösung	Punkte
		5.00
Base case: `grt (add n (Succ Zero)) n`	Base case: `grt (add Zero (Succ x)) Zero`	0.00
	`= True` by def. `grt`	0.00
Inductive step: `grt (add (Succ n) (Succ x)) (Succ n)`	Inductive step: `grt (add (Succ n) (Succ x)) (Succ n)`	1.00
`= grt (Succ (add n (Succ x))) (Succ n)` by def. `add`	`= grt (Succ (add n (Succ x))) (Succ n)` by def. `add`	0.50
`= grt (Succ (add x n)) n` by def. `add`	`= grt (add n (Succ x)) n` by def. `grt`	0.00
`= grt (Succ (add Zero n)) n` by def. `add`	`= True` by hyp.	0.00
`= grt (Succ n) n` by def. `add`		0.00
`= True` by def. `grt`		0.00
		Total: 1.50

(a) Student A

Ihre Antwort	Lösung	Punkte
		5.00
Base case: `grt (add Zero (Succ x)) Zero`	Base case: `grt (add Zero (Succ x)) Zero`	1.00
`= grt (Succ x) Zero` by def. `grt`	`= True` by def. `grt`	0.00
Inductive step: `grt (add (Succ Zero) (Succ x)) (Succ Zero)`	Inductive step: `grt (add (Succ n) (Succ x)) (Succ n)`	0.00
`= grt (Succ (Succ x)) (Succ Zero)` by def. `add`	`= grt (Succ (add n (Succ x))) (Succ n)` by def. `add`	0.00
`= True` by def. `grt`	`= grt (add n (Succ x)) n` by def. `grt`	0.00
	`= True` by hyp.	0.00
		Total: 1.00

(b) Student B

Figure 5: No unfair grading with new algorithm

- Evaluation algorithm based on **correct sequences with predefined entry points**

Summary & Future Work

- Today: Glimpse of preliminary analysis, proof & programming tasks
- What else?
  - Checking code snippets with regular expressions
  - Flexibly generating suitable regular expressions
  - General-purpose comment field for each task
  - Evaluation
    - Degree of automation
    - Student view
    - Examiner view
- Future:
  - Improve awarding partial points
  - Automatically generate most of the exam from a single literate Haskell file with Markdown